

John Eyre and Fiona Hilton

Met Office, UK



Beyond optimal estimation: sensitivity of analysis error to misspecification of background error

- Motivation
- Theory of analysis/retrieval error
 - optimal estimation
 - sub-optimal case
- Illustration
 - scalar case
 - IASI example
- Conclusions and further work



Motivation (1)

What improvements are needed to exploit advanced IR sounder data more fully in NWP?

- Efficient processing of the full spectrum
- Observation errors, including correlations
- Residual biases
- Surface properties over land and ice
- Background error statistics
- Treatment of cloud



Motivation (2)

- Optimal estimation (OE) theory
 - ... assumes the error covariances are known.
 - In practice, they are not known.
- → 2 ways forward:
 - improve estimates of covariances continuing work
 - make assimilation/retrieval robust against our inevitable lack of knowledge
- Applies to both background and obs error covs, B and R
 - in this presentation, only B considered



Motivation (3)

- Why is B inevitably in error?
 - global averages can be estimated quite accurately
 - ... but large spatial/temporal variability.
- We need to understand our sensitivity to B and its inevitable mis-specification,
 - particularly for satellite radiances ...
 - non-local observations (→ Fiona Hilton's paper)



Motivation (4)

- Advanced IR sounders have vertical resolution ~ 1 km
 - sensitive with low error to scales »1 km
 - not sensitive to scales «1 km
 - sensitive to scales ~ 1 km, but with errors comparable to background errors
- → Need to understand B its magnitude on different scales
 - determines how measurements and prior information are weighted on each scale
- → ... and effects of mis-specifying B on each scale



GENERAL CASE

Analysis equation (linearised): $x^a = x^b + K \cdot (y^o - H[x^b])$

Analysis error equation: $\varepsilon^a = \varepsilon^b + K \cdot (\varepsilon^o - H \cdot \varepsilon^b)$

$$\varepsilon^{a} = (I-K.H). \varepsilon^{b} + K. \varepsilon^{o}$$

Analysis error covariance: $A = (I-K.H).B.(I-K.H)^T + K.R.K^T$

OPTIMAL CASE

assumed value B_A = true value B

$$K = B_A.H^T.(H.B_A.H^T+R)^{-1}$$
 $A_{OPT} = (I-K.H). B_A.(I-K.H)^T + K.R.K^T$
 $= (I-K.H).B_A$
 $A_{OPT}^{-1} = B_A^{-1} + H^T.R^{-1}.H$

Projecting on to the eigenvectors of B_A :

V = eigenvectors of B_A : Λ = eigenvalues of B_A

$$A_{OPT}^{-1} = B_A^{-1} + H^T.R^{-1}.H$$
 $V^T.A_{OPT}^{-1}.V = V^T.B_A^{-1}.V + V^T.H^T.R^{-1}.H.V$
 $V^T.A_{OPT}^{-1}.V = \Lambda^{-1} + V^T.H^T.R^{-1}.H.V$

Why B_△?

- because this is what we use the "filter" within the DA system
 - Met Office 4D-Var performs vertical analysis in this eigen-space



OPTIMAL

$$A_{OPT}(B) = (I-K.H). B .(I-K.H)^T + K.R.K^T$$
 $K(B) = B.H^T.(H.B.H^T+R)^{-1}$

GENERAL / SUB-OPTIMAL, which means $B \neq B_A$, $K=K(B_A)$

$$A(B) = (I-K(B_A).H).B.(I-K(B_A).H)^T + K(B_A).R.K(B_A)^T$$

$$A(B) = A_{OPT}(B_A) + (I-K(B_A).H).(B-B_A).(I-K(B_A).H)^T$$

Note: linear in B



Illustration – scalar case (1)

$$H = 1$$

 $R = 1$
 $B_A = 1$

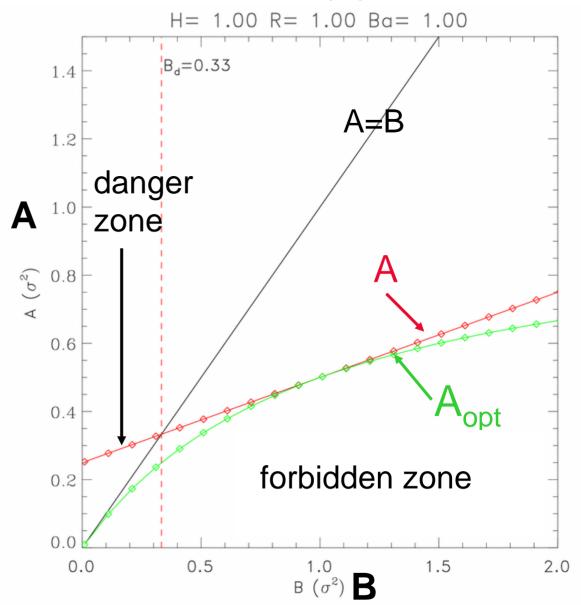




Illustration – scalar case (2)

H = 1 R = 2.72 $B_A = 1$

higher observation error

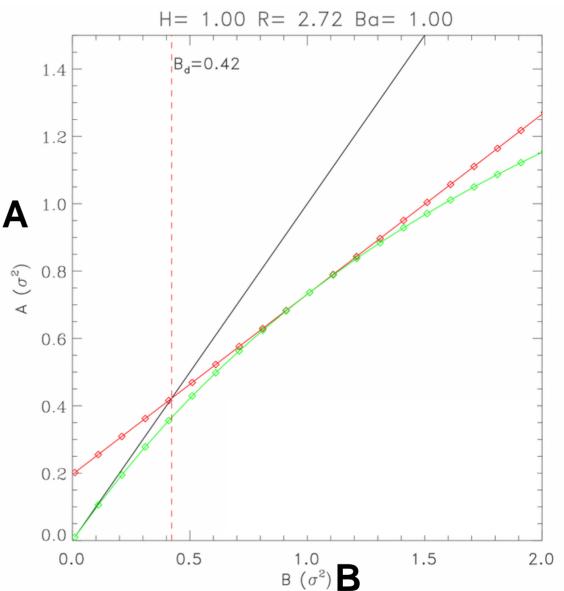
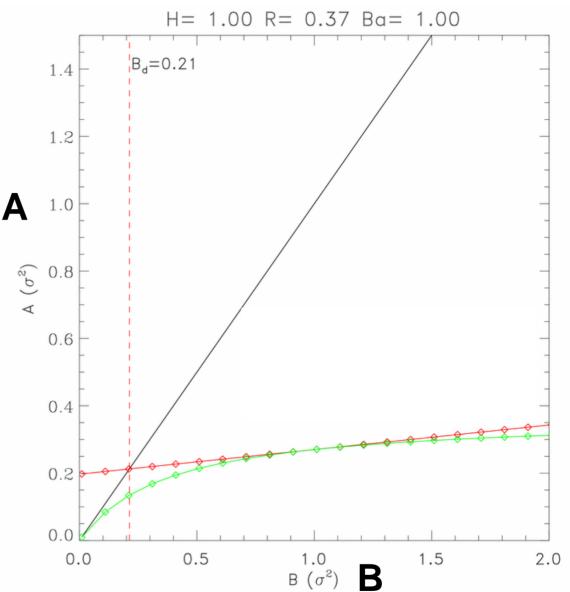




Illustration – scalar case (3)

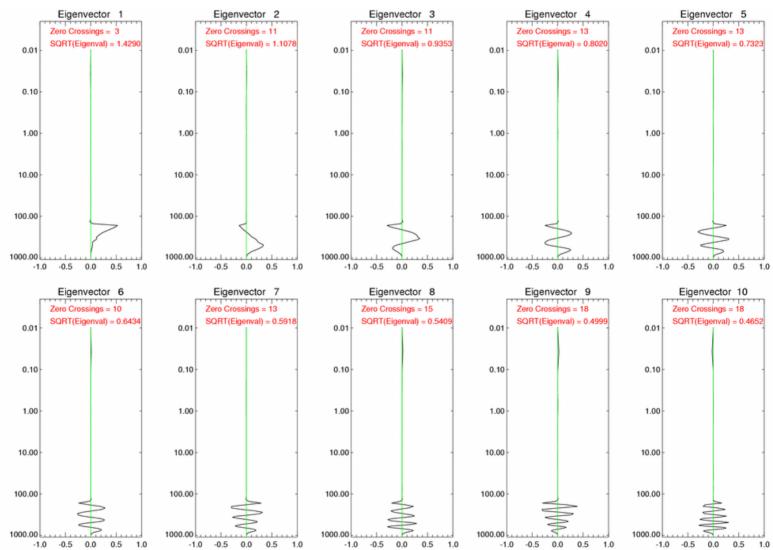
H = 1 R = 0.37 $B_A = 1$

lower observation error



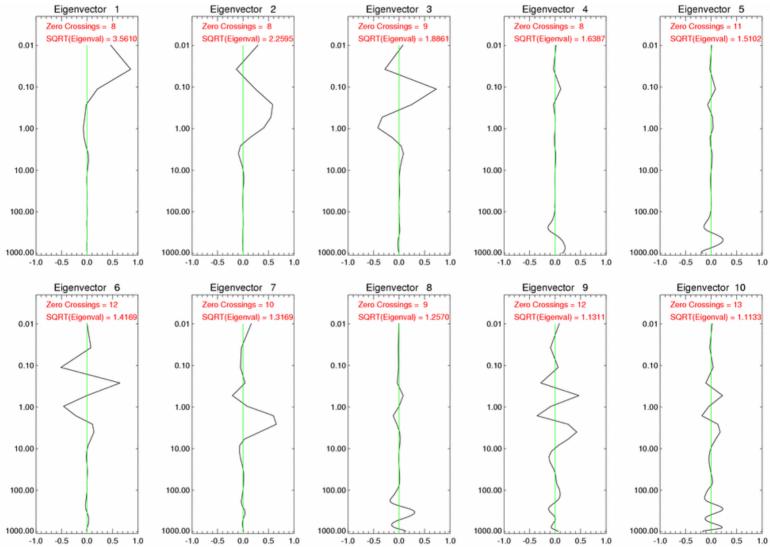


Leading eigenvectors of B_A MetO 70-level model, ln(q) (vectors 1-10)





Leading eigenvectors of B_A MetO 70-level model, temp. (vectors 1-10)





Leading eigenvectors of B_A MetO 70-level model, temp. (vectors 11-20)

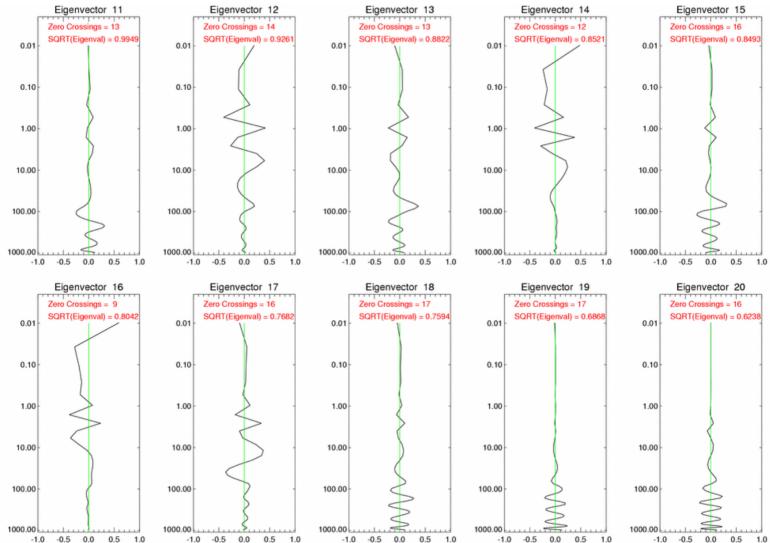




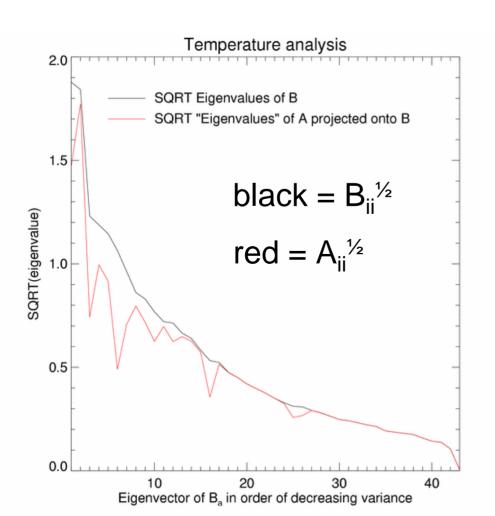
Illustration – IASI (1)

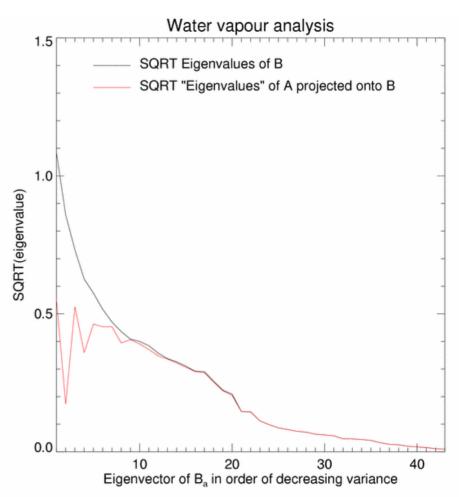
- Met Office operational 1D-var channel selection
 - 183 channels, of which 31 in water vapour band
- Observation error
 - instrument noise, or
 - instrument noise + forward model error of 0.2K + extra for unmodelled trace gas
- Analysis on 43 RTTOV levels using Jacobians from US standard atmosphere



Diagonal of analysis error mapped to eigenvectors of B_A

observation error = instrument noise + forward model error

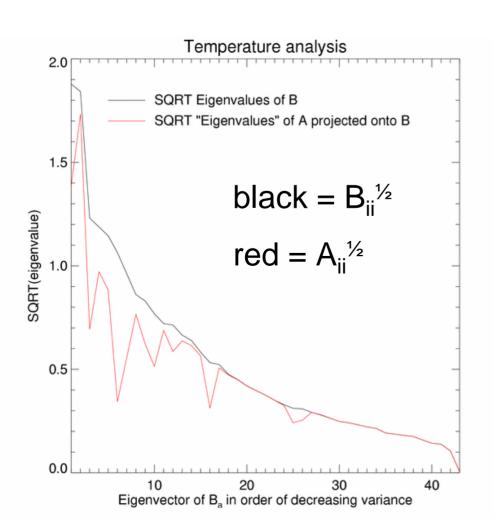


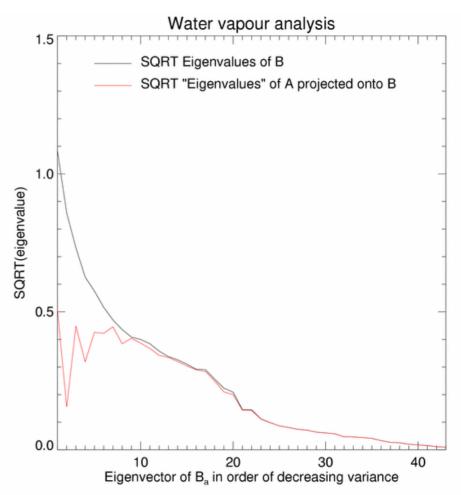




Diagonal of analysis error mapped to eigenvectors of B_A

observation error = instrument noise







Conclusions so far ...

- Goal: make retrievals/analyses robust against inevitable errors in the background error covariance
- ... particularly for effective assimilation of satellite sounder data
- What is crucial for NWP? structure of B assumed by the DA system, B_A
- Beware the danger zone! analysis errors higher than background errors
- Current problems with Met Office 4D-Var B-matrix for temperature
- (provisional result) Some real IASI information is currently filtered out by the assimilation system



- Further work needed:
 - to perform a more complete error analysis for IASI
 - to understand B_A on each scale | good idea, in general
 - ... and to improve it
 - to make B_A robust against inevitable errors



Thank you! Questions?

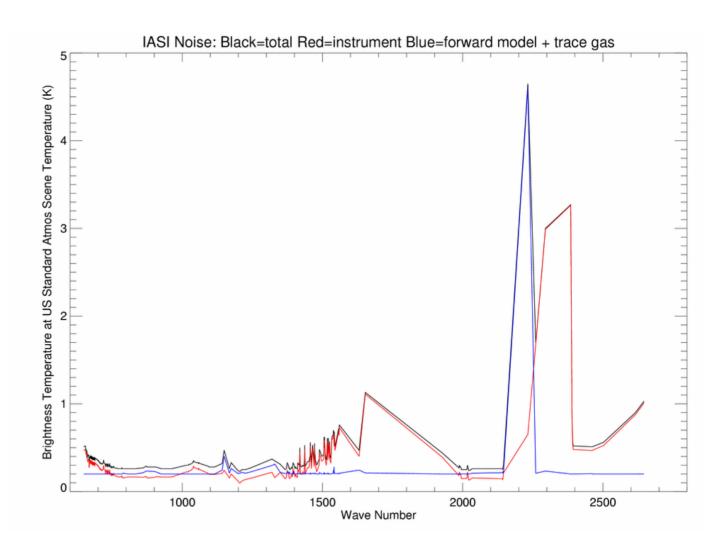


IASI noise

black: total

red: instrument

blue: forward model + "trace gas noise"





Goal

- To exploit the improved vertical resolution of advanced IR sounders
- ... whilst retaining the (usually accurate) information from the NWP model on sharp vertical structures
 - e.g. PBL top, tropopause

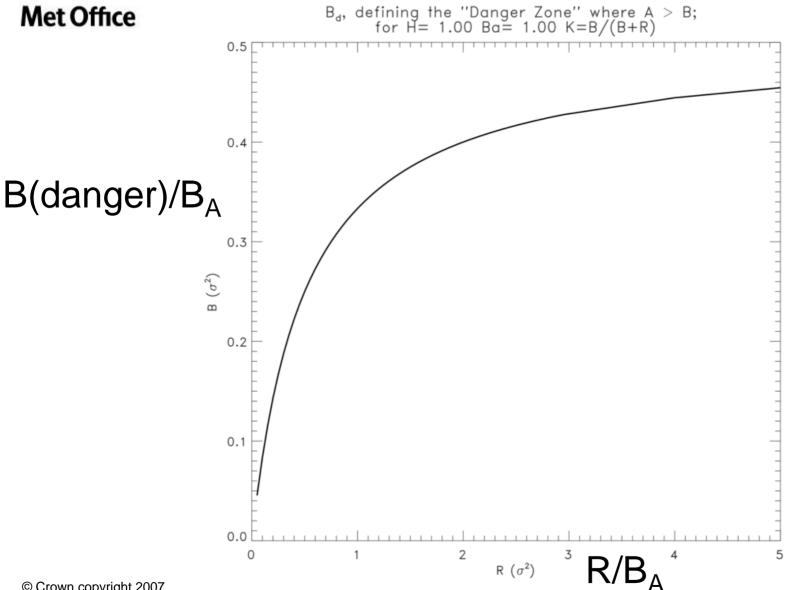


Prior work on mis-specification of errors

- O.N.Strand 1977 The Annals of Statistics
- R.Daley 1991 Atmospheric Data Assimilation
 - R.Seaman 1977 MWR
 - R.Seaman et al. 1983 Aus. Met. Mag.
 - R.Franke 1985 MWR
- P.Watts and A.McNally 1988 Proc. ITSC-IV
- A.McNally 2000 QJRMS
- Others?



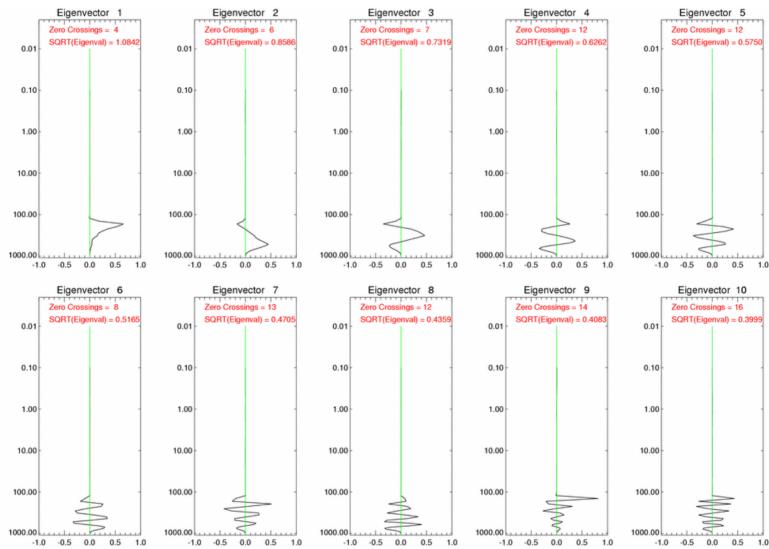
Scalar case – the danger zone





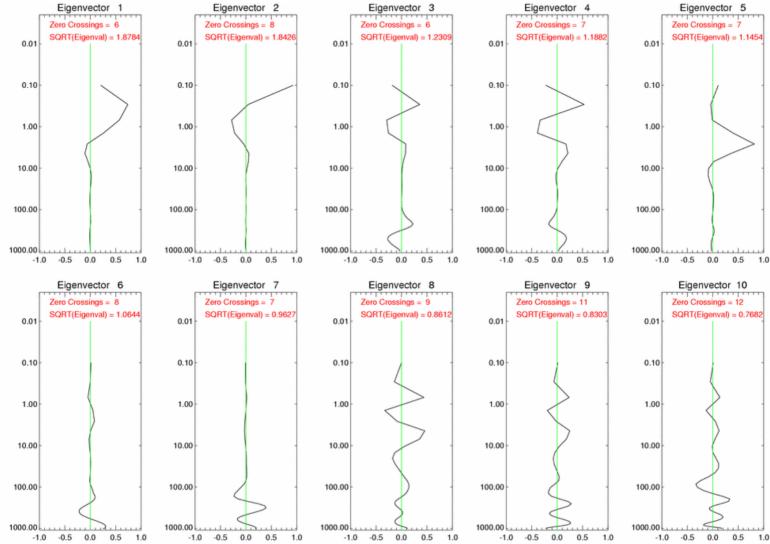
© Crow

Leading eigenvectors of B_A 43 RTTOV levels ln(q) (vectors 1-10)



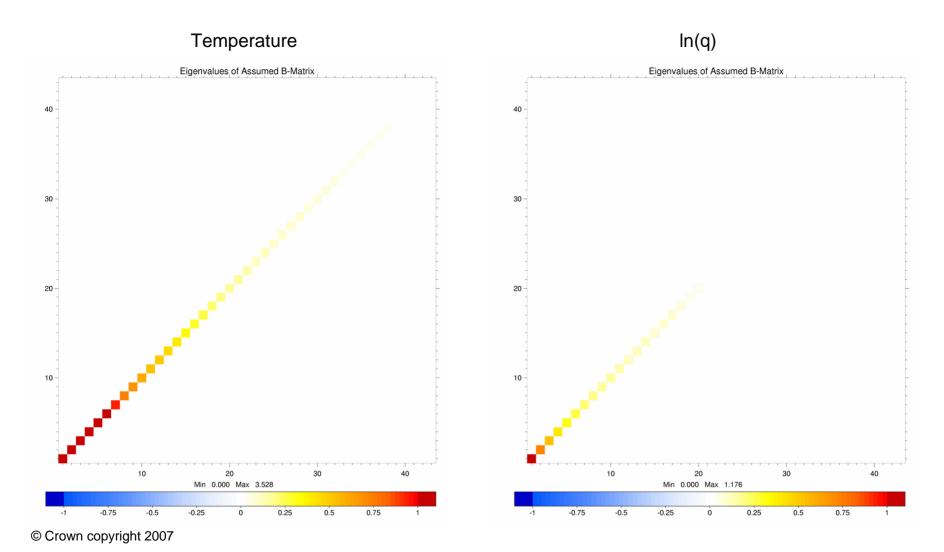


Leading eigenvectors of B_A 43 RTTOV levels temperature (vectors 1-10)



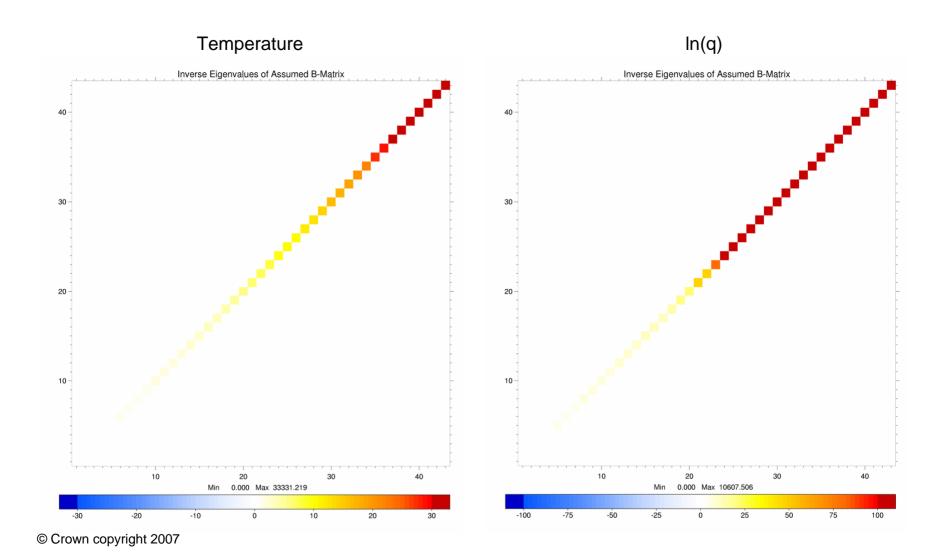


Eigenvalues of B_A: background errors in the eigenspace of B_A





Inverse eigenvalues of B_A

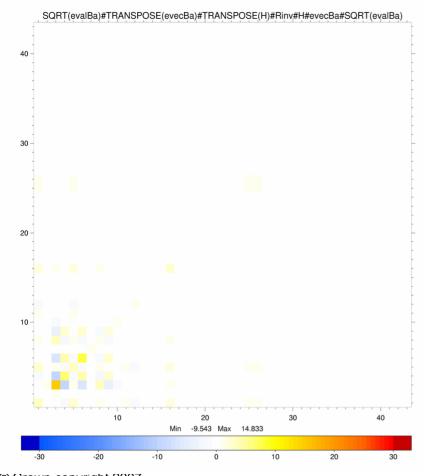


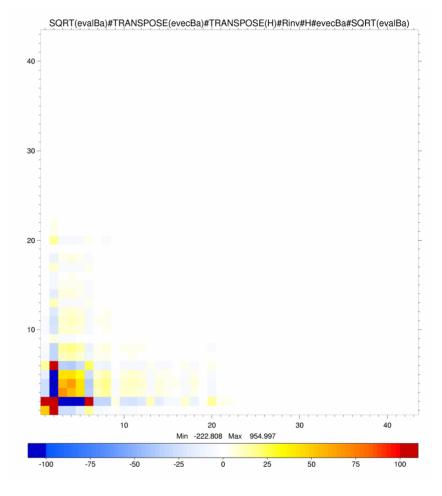


IASI information mapped to B_A eigenvectors and normalised by B_A eigenvalues:

 $\Lambda^{\frac{1}{2}}.V^{T}.H^{T}.R^{-1}.H.V.\Lambda^{\frac{1}{2}}$

Temperature Instrument noise + forward model error In(q)







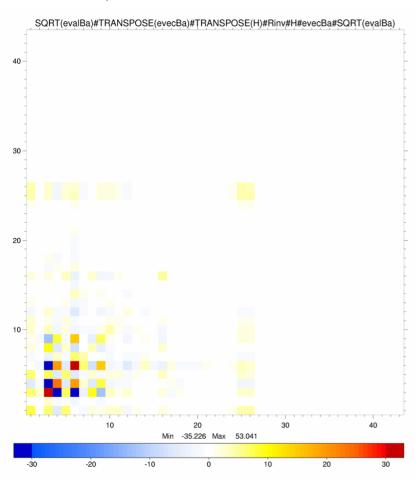
IASI information mapped to B_A eigenvectors and normalised by B_A eigenvalues:

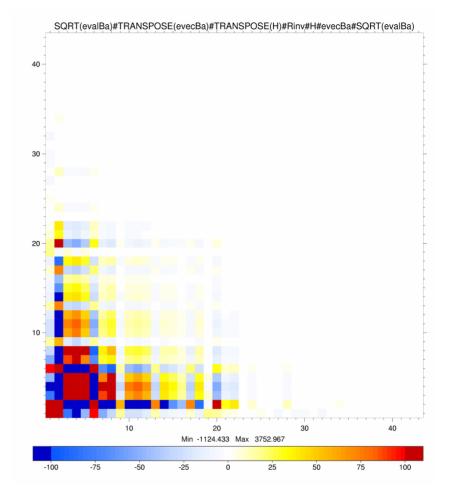
 $\Lambda^{\frac{1}{2}}.V^{T}.H^{T}.R^{-1}.H.V.\Lambda^{\frac{1}{2}}$

Temperature

Instrument noise only



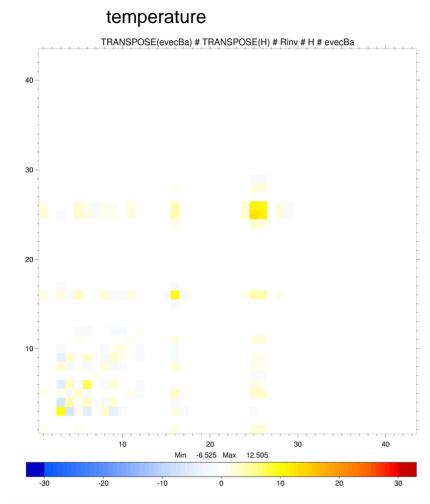


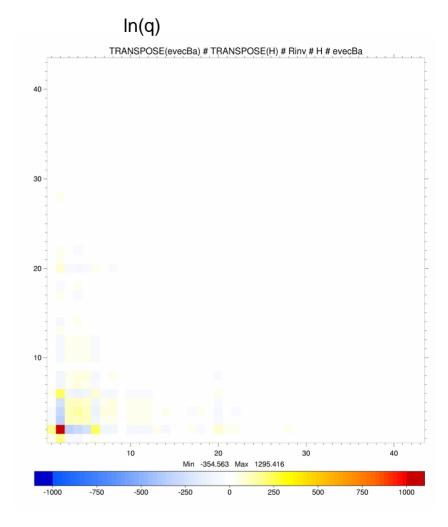




IASI observation error mapped to eigenvectors of B_A : $V^T.H^T.R^{-1}.H.V$

observation error = instrument noise + forward model error







IASI observation error mapped to eigenvectors of B_A

observation error = instrument noise only

